Combinatorial optimization

The guiding question of Combinatorial Optimization is: How do I efficiently select an optimal solution among a finite but very large set of alternatives? We will address the solution of this question in the context of classical discrete optimization problems.

Content

• Paths and flows: Strongly polynomial time algorithms for shortest paths and minimum cost network flows
• Minimum spanning trees and matroids: Greedy, Kruskal’s and Prim’s algorithm
• Arborescences and matroid intersection
• Polyhedra and approximation algorithms
• Maximum weight matchings in general graphs and the matching polytope

Keywords

• Algorithm
• Polyhedron
• Matroid
• NP-completeness

Learning Prerequisites

Required courses
Discrete optimization (Second year math.)

Learning Outcomes

By the end of the course, the student must be able to:

• Choose an appropriate method for solving a combinatorial optimization problem
• Prove theorems in discrete optimization
• Design algorithms
• Analyze efficiency of algorithms

Transversal skills
• Demonstrate a capacity for creativity.
• Continue to work through difficulties or initial failure to find optimal solutions.
• Assess one's own level of skill acquisition, and plan their on-going learning goals.

Teaching methods
Ex cathedra lecture and exercises to be solved at home and in the classroom

Expected student activities
Attendance of lectures and exercises
Completion of exercises at home
Study of literature

Assessment methods
Written exam during exam session

Supervision
Office hours Yes
Assistants Yes
Forum No

Resources
Bibliography