### Remarque

This course focuses on the foundational, discrete mathematics core of advanced computation.

### Summary

Discrete mathematics is a discipline with applications to almost all areas of study. It provides a set of indispensable tools to computer science in particular. This course reviews (familiar) topics as diverse as mathematical reasoning, combinatorics, discrete structures & algorithmic thinking.

### Content

I. Mathematical reasoning: propositional logic, propositional functions, quantifiers, rules of inference; this includes very basic logic circuits.  
II. Sets and counting: cardinalities, inclusion/exclusion principle, sequences and summations.  
III. Algorithms and complexity: basic algorithms, computational complexity, big-O notation and variants, countability.  
IV. Number representations such as binary and hexadecimal and (postponed to 2nd semester) basic number theory: modular arithmetic, integer division, prime numbers, hash functions, pseudorandom number generation; applications.  
V. Induction and recursion: mathematical induction, recursive definitions and algorithms.  
VI. Basic combinatorial analysis: permutations, binomial theorem, basic generating functions.  
VII. Basic probability: events, independence, random variables, Bayes’ theorem.  
VIII. Structure of sets: relations, equivalence relations, power set.  
IX. (time permitting) Elementary graph theory: graphs, Euler and Hamilton paths, Dijkstra’s algorithm, spanning trees.

### Keywords

Propositional logic, counting, complexity, big-O, number representations, sets, matrices, modular arithmetic, induction, basic probabilities, Bayes theorem, combinatorial analysis, recurrences, generating functions, countability, graph theory.

### Learning Outcomes

By the end of the course, the student must be able to:

- Recognize if there is a mistake in a (simple) proof  
- Apply general problem-solving techniques  
- Recognize the mathematical structures present in applications  
- Apply simple recursion and use it to design recursive algorithms  
- Apply the tools studied in class to solve problems  
- Demonstrate familiarity with mathematical reasoning  
- Solve linear recurrences and use generating functions  
- Argue about (un)countability  
- Formulate complete, clear mathematical proofs
Transversal skills

• Assess one's own level of skill acquisition, and plan their on-going learning goals.
• Continue to work through difficulties or initial failure to find optimal solutions.
• Demonstrate the capacity for critical thinking

Teaching methods

Ex cathedra (blackboard) lectures

Expected student activities

Studying the book, test your understanding by making the exercises, ask questions

Assessment methods

Final exam (100%), mostly (and possibly exclusively) multiple choice

Supervision

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<tr>
<th>Office hours</th>
<th>No</th>
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<tbody>
<tr>
<td>Assistants</td>
<td>Yes</td>
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<td>Forum</td>
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| Others       | A list of students assistants and their contact data will be made available on the moodle page for this course, along with an assignment of each registered student to one of the student assistants.

If you have a question, first contact the student assistant assigned to you. If that does not help, contact one of the teaching assistants (Marguerite Delcourt, Dusan Kostic and Benjamin Wesolowski). Furthermore, you are always welcome to stop by at my office (INJ330, no office hours, I'm available when I'm there) for any type of question related to this course or your study at EPFL.

Never hesitate to ask questions before, during or after the lectures!

Resources

Bibliography

"Discrete Mathematics and Its Applications", Kenneth H. Rosen, 7th ed, McGraw-Hill 2012. (You should be able to find the pdf on the web.)

Ressources en bibliothèque

• Discrete mathematics and its applications / Rosen

Websites

• http://will be provided later, if any

Moodle Link

• http://will be provided later