MATH-451 **Numerical approximation of PDE's I**

Nobile Fabio

Cursus	Sem.	Type
Computational science and Engineering	MA2, MA4	Opt.
Financial engineering	MA2, MA4	Opt.
Mathematics	BA6	Opt.

Language of teaching	English
Credits	5
Session	Summer
Semester	Spring
Exam	Written
Workload	150h
Weeks	14
Hours	**4 weekly**
Courses	2 weekly
Exercises	2 weekly
Number of positions	

Summary

The aim of the course is to give a theoretical and practical knowledge of finite difference and finite element methods for the numerical approximation of partial differential equations in one or more dimensions.

Content

- Finite difference methods for elliptic, parabolic and hyperbolic equations; stability and convergence analysis
- Linear elliptic problems: weak form, well-posedness, Galerkin approximation
- Finite element approximation in two and three dimensions: stability, convergence, a-priori error estimates in different norms, implementation aspects
- Transport dominated problems and stabilization techniques

Keywords

Partial Differential Equations, Finite difference method, Finite element method, Galerkin approximation, convergence analysis.

Learning Prerequisites

Required courses

Analysis I-II-III-IV, Numerical analysis

Recommended courses

Functional Analysis I, Introduction aux équations aux dérivées partielles, Measure and Integration, Programming

Important concepts to start the course

- Basic knowledge of functional analysis, Banach and Hilbert spaces, L^p spaces.
- Some knowledge on theory of elliptic PDEs, weak solutions, existence and uniqueness.
- Basic concepts in numerical analysis: stability, convergence, condition number, solution of linear systems, quadrature formulae, polynomial interpolation.

Learning Outcomes

By the end of the course, the student must be able to:

- Choose an appropriate discretization scheme to solve a specific PDE
- Analyze numerical errors
- Interpret results of a computation in the light of theory
- Prove theoretical properties of discretization schemes
- Solve a PDE using available software
- State theoretical properties of PDEs and corresponding discretization schemes
- Describe discretization methods for PDEs

Transversal skills

- Use a work methodology appropriate to the task.
- Use both general and domain specific IT resources and tools
- Write a scientific or technical report.

Teaching methods

Ex cathedra lectures, exercises in the classroom and computer lab sessions

Expected student activities

- Attendance of lectures
- Completing exercicies
- Solving simple problems on the computer

Assessment methods

written exam. The exam may involve the use of a computer.
Dans le cas de l'art. 3 al. 5 du Règlement de section, l'enseignant décide de la forme de l'examen qu'il communique aux étudiants concernés.

Supervision

Office hours	Yes
Assistants	Yes
Forum	No

Resources

Virtual desktop infrastructure (VDI)

Yes

Bibliography

- A.Quarteroni, Numerical Models for Differential Problems, Springer, 2009
- S.C. Brenner, L.R. Scott The Mathematical Theory of Finite Element Methods, Springer, 3rd ed, 2007
- A. Ern, J-L. Guermond, Theory and Practice of Finite Elements, Springer, 2004
- Lecture notes by the teacher

Ressources en bibliothèque

- The Mathematical Theory of Finite Element Methods / Brenner

- Numerical Models for Differential Problems / Quarteroni
- Theory and Practice of Finite Elements / Ern

Moodle Link

- http://moodle.epfl.ch/

Prerequisite for

Numerical Approximation of Partial Differential Equations II