

COM-514

Mathematical foundations of signal processing

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Cursus	Sem.	Type
Communication systems minor	H	Opt.
Computational science and Engineering	MA1, MA3	Opt.
Computer and Communication Sciences		Obl.
Computer science	MA1, MA3	Opt.
Data Science	MA1	Opt.
SC master EPFL	MA1, MA3	Opt.
Systems Engineering minor	H	Opt.

Language of teaching	English
Credits	6
Session	Winter
Semester	Fall
Exam	Written
Workload	180h
Weeks	14
Hours	5 weekly
Courses	3 weekly
Exercises	2 weekly
Number of positions	

Summary

Signal processing tools are presented from an intuitive geometric point of view which is at the heart of all modern signal processing techniques. Student will develop the mathematical depth and rigor needed for the study of advanced topics in signal processing.

Content

From Euclid to Hilbert (vector spaces; Hilbert spaces; approximations, projections and decompositions; bases)

Sequences and Discrete-Time Systems (sequences; systems; discrete-time Fourier transform; z-transform; DFT; multirate sequences and systems; filterbanks)

Functions and Continuous-Time Systems (functions; systems; Fourier transform; Fourier series)

Sampling and Interpolation (sampling and interpolation with finite-dimensional vectors, sequences, functions and periodic functions)

Approximation and Compression (approximation by polynomials, splines, and series truncation)

Localization and Uncertainty (localization for functions, sequences and bases; local Fourier and wavelet bases; time, frequency and resolution in the real world)

Compressed Sensing (overview and definitions; reconstruction methods and applications)

Learning Prerequisites**Required courses**

Circuits and Systems

Recommended courses

Signal processing for communications

Learning Outcomes

By the end of the course, the student must be able to:

- Master the right tools to tackle advanced signal and data processing problems
- Develop an intuitive understanding of signal processing through a geometrical approach
- Get to know the applications that are of interest today
- Learn about topics that are at the forefront of signal processing research

Teaching methods

Ex cathedra with exercises

Expected student activities

Attending lectures, completing exercises

Assessment methods

Homeworks 20%, midterm (written) 30%, final exam (written) 50%

Supervision

Office hours	Yes
Assistants	Yes
Forum	No

Resources

Virtual desktop infrastructure (VDI)

No

Bibliography

M. Vetterli, J. Kovacevic and V. Goyal, "*Signal Processing: Foundations*", Cambridge U. Press, 2014.
Available in open access at <http://www.fourierandwavelets.org>

Ressources en bibliothèque

- [Signal Processing: Foundations / Vetterli](#)

Websites

- http://lcav.epfl.ch/SP_Foundations

Moodle Link

- <http://moodle.epfl.ch/course/view.php?id=13431>