MATH-371	Homology and cohomology

Sem.	Туре	Language of	English
BA6	Opt.	Language of teaching Credits Session Semester Exam Workload Weeks Hours Courses Exercises Number of positions	English 5 Summer Spring Written 150h 14 <b>4 weekly</b> 2 weekly 2 weekly
	Sem. BA6	Sem.TypeBA6Opt.	Sem.TypeBA6Opt.Language of teaching Credits Session Semester Exam Workload Weeks Hours Courses ExercisesHours Courses ExercisesNumber of positions

## Summary

This course introduces to homology and cohomology of topological spaces and groups as well as their relation via the classifying space of a group.

## Content

- 1. Simplicial homology
- 2. Singular homology
- 3. Cellular homology
- 4. Abstract homology theories
- 5. Cohomology
- 6. Group homology and cohomology
- 7. Classifying spaces

# Keywords

algebraic topology, group cohomolgy, homological algebra, classifying spaces

# Learning Prerequisites

Required courses

- Topology (MATH-225)
- Rings and fields (MATH-215)

# **Recommended courses**

- Rings and modules (MATH-311)
- Group theory (MATH-211)

# Learning Outcomes

By the end of the course, the student must be able to:

- Compare (co)homology theories of spaces
- Use basic algebraic homological algebra
- Choose appropriate methods to compute (co)homology



- Compute (co)homology
- Characterize low degree (co)homology of groups
- Compute models for classifying spaces

#### **Transversal skills**

- Continue to work through difficulties or initial failure to find optimal solutions.
- Demonstrate the capacity for critical thinking
- Access and evaluate appropriate sources of information.
- Write a scientific or technical report.
- Use both general and domain specific IT resources and tools
- Take feedback (critique) and respond in an appropriate manner.
- Give feedback (critique) in an appropriate fashion.

## **Teaching methods**

Ex-cathedra course with exercises in the classroom and at home

#### **Expected student activities**

- Participate in the course and the exercise sessions
- Solve regular exercises
- Prepare one LaTeX hand-in on examples illustrating the course content
- Give peer-feedback on this LaTeX hand-in
- Prepare one LaTeX hand-in on a short piece of mathematics acquired independently

## **Assessment methods**

Written exam, exercises, LaTeX hand-ins and peer-feedback. In case Art. 3 al. 5 of the regulations of the section apply to some student, the exam form will be decided by the teacher and communicated to the student.

#### Supervision

Office hours	Yes
Assistants	Yes
Forum	No

#### Resources

Bibliography

- Allen Hatcher. Algebraic topology. ISBN-13: 978-0-521-79540-1
- Kenneth S. Brown. Cohomology of groups. ISBN-13: 3-540-90688-6
- Charles A. Weibel. An introduction to homological algebra. ISBN-13: 0-521-55987-1

#### Ressources en bibliothèque

- Algebraic topology / Hatcher
- (electronic version)
- Cohomology of groups / Brown
- An introduction to homological algebra / Weibel
- (electronic version)