

MATH-405

**Harmonic analysis**

Krieger Joachim

Cursus	Sem.	Type
Ing.-math	MA2, MA4	Opt.
Mathématicien	MA2	Opt.

Language of teaching	English
Credits	5
Session	Summer
Semester	Spring
Exam	Oral
Workload	150h
Weeks	14
<b>Hours</b>	<b>4 weekly</b>
Courses	2 weekly
Exercises	2 weekly
<b>Number of positions</b>	

**Summary**

An introduction to methods of harmonic analysis. Covers convergence of Fourier series, Hilbert transform, Calderon-Zygmund theory, Fourier restriction, and applications to PDE.

**Content**

- Fourier series, convergence and summability.
- Fourier series, convergence and summability.
- Hilbert transform.
- Calderon-Zygmund theory of singular integrals.
- Littlewood-Paley theory.
- Fourier restriction.
- Applications to dispersive PDE.

**Keywords**

Fourier series, convergence, singular integrals, Calderon-Zygmund theory, Fourier restriction.

**Learning Prerequisites****Required courses**

Analyse I - IV, Algebre lineaire I et II.

**Recommended courses**

Analyse I - IV, Algebre lineaire I et II.

**Important concepts to start the course**

Understand key concepts of real analysis, such as measure and Lebesgue integral. Be able to construct a rigorous mathematical argument.

**Learning Outcomes**

By the end of the course, the student must be able to:

- Analyze convergence of Fourier series
- Examine bounds for singular integrals
- Prove bounds for dispersive PDE

**Transversal skills**

- Communicate effectively with professionals from other disciplines.
- Access and evaluate appropriate sources of information.
- Give feedback (critique) in an appropriate fashion.

**Teaching methods**

Two hours ex cathedra lectures, two hours of exercises led by teaching assistant.

**Expected student activities**

Attend lectures and exercise sessions, read course materials, solve exercises.

**Assessment methods**

Oral exam at the end of course.

Dans le cas de l'art. 3 al. 5 du Règlement de section, l'enseignant décide de la forme de l'examen qu'il communique aux étudiants concernés.

**Supervision**

Office hours	No
Assistants	Yes
Forum	No

**Resources****Bibliography**

- Classical multilinear harmonic analysis by C. Muscalu and W. Schlag.
- Singular integrals and differentiability properties of functions by E. Stein.

**Notes/Handbook**

No.

**Websites**

- <http://pde.epfl.ch>