**Summary**

Linear and nonlinear dynamical systems are found in all fields of science and engineering. After a short review of linear system theory, the class will explain and develop the main tools for the qualitative analysis of nonlinear systems, both in discrete-time and continuous-time.

**Content**

- **Introduction**: Dynamics of linear and non-linear systems. Definitions; Unicity of a solution; Limit Sets, Attractors.
- **Linear Systems**: Solutions; Stability of autonomous systems, Geometrical analysis, connection with frequency domain analysis.

- The class is methodology-driven. It may present some limited examples of applications, but it is not application-driven.

**Keywords**


**Learning Prerequisites**

**Required courses**

- Linear algebra (MATH 111 or equivalent).
- Analysis I, II, III (MATH 101, 106, 203 or equivalent).
- Circuits & Systems II (EE 205 or equivalent) or a Systems & Signals class (MICRO 310/311 or equivalent).

**Recommended courses**
• A first-year Probability class, such as MATH-232, MATH-231, MATH-234(b), MATH-234(c), or equivalent.
• Analysis IV (MATH 207 or equivalent)

Important concepts to start the course
• Linear Algebra (vector spaces, matrix operations, including inversion and eigendecomposition).
• Calculus (linear ordinary differential equations; Fourier, Laplace and z-Transforms).
• Basic notions of topology.
• Basic notions of probability.

Learning Outcomes
By the end of the course, the student must be able to:
• Analyze a linear or nonlinear dynamical system.
• Anticipate the asymptotic behavior of a dynamical system.
• Assess / Evaluate the stability of a dynamical system.
• Identify the type of solutions of a dynamical system.

Teaching methods
• Lectures (blackboard), 2h per week
• Exercise session, 1h per week.

Expected student activities
Exercises in class and at home (paper and pencil, and Matlab)

Assessment methods
1. Mid-term 20% (conditionally on the Covid situation allowing for it to be taken at EPFL).
2. Final exam 80%

Supervision
| Office hours | Yes |
| Assistants   | Yes |
| Forum        | Yes |

Resources
Bibliography
Course notes; textbooks given as reference on the moodle page of the course.

Notes/Handbook
Course notes, exercises and solutions provided on the moodle page of the course.

Moodle Link
• https://go.epfl.ch/COM-502

Prerequisite for
Classes using methods from dynamical systems.