

MATH-467

Probabilistic methods in combinatorics

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Cursus	Sem.	Type
Ing.-math	MA2, MA4	Opt.
Mathématicien	MA2	Opt.

Language of teaching	English
Credits	5
Session	Summer
Semester	Spring
Exam	Written
Workload	150h
Weeks	14
Hours	4 weekly
Courses	2 weekly
Exercises	2 weekly
Number of positions	

Summary

The 'probabilistic method' is a fundamental tool in combinatorics. The basic idea is as follows: to prove that an object (for example, graph) with certain properties exists, it suffices to prove that if the object is chosen at random, then it has the desired properties with positive probability.

Content

In this course we will cover the following topics:

- the basic probabilistic method
- the method of alterations
- the second moment method
- Chernoff bound and martingale concentration inequalities
- Lovasz Local Lemma
- correlation inequalities
- Janson's inequality

In each section of the course, the corresponding method will be presented through several examples and applications; usually, but not exclusively, in the context of graph theory and combinatorial number theory.

Keywords

probabilistic method, random graphs, concentration inequalities, expected value, variance

Learning Prerequisites**Recommended courses**

Graph theory (MATH-360)

Important concepts to start the course

Familiarity with basic concepts of probability theory and graph theory are essential for this course. In particular, the student should be comfortable with the following notions from these subjects:

- random variable
- independence
- expectation
- variance, covariance

- complete graph
- subgraph
- paths, trees, cycles
- clique, independent set
- chromatic number

The first exercise class will be devoted to recalling the necessary background in probability theory and graph theory.

Learning Outcomes

By the end of the course, the student must be able to:

- Apply the probabilistic method to solve problems
- Choose which version of the method will be suited to the problem
- Prove the main results of the course
- Modify the main proofs if needed, to prove similar results

Teaching methods

In-person lectures + in-person exercise classes covering weekly exercise sheets.

Expected student activities

The students are expected to attend the lectures and the exercise classes. In addition, they are expected to attempt the problems on the exercise sheets and to submit their solutions of a selected subset of the exercises for grading.

Assessment methods

Written final exam

Supervision

Office hours	Yes
Assistants	Yes
Forum	Yes

Resources

Bibliography

Noga Alon and Joel H. Spencer. *The probabilistic method*. John Wiley & Sons, 2016.

Notes/Handbook

Lecture notes will be provided.

Moodle Link

- <https://go.epfl.ch/MATH-467>